
IDP-Z3

Pierre Carbonnelle

Oct 14, 2021

CONTENTS:

| | | |
|----------|---|-----------|
| 1 | Introduction | 1 |
| 1.1 | Installation using poetry | 1 |
| 1.2 | Installation using pip | 2 |
| 1.3 | Installation of idp_engine module | 2 |
| 2 | The IDP Language | 5 |
| 2.1 | Overview | 5 |
| 2.2 | Shebang | 6 |
| 2.3 | Vocabulary | 6 |
| 2.4 | Theory | 8 |
| 2.5 | Structure | 10 |
| 2.6 | Main block | 11 |
| 2.7 | Differences with IDP3 | 13 |
| 2.8 | Syntax summary | 13 |
| 3 | Python API | 17 |
| 3.1 | IDP class | 17 |
| 4 | Command Line Interface | 19 |
| 5 | Interactive Consultant | 21 |
| 5.1 | Display | 21 |
| 5.2 | Vocabulary annotations | 22 |
| 5.3 | Environment | 22 |
| 5.4 | Default Structure | 23 |
| 6 | Appendix: IDP-Z3 developer reference | 25 |
| 6.1 | Architecture | 25 |
| 6.2 | idp_engine module | 30 |
| 6.3 | idp_server module | 50 |
| 7 | Index | 53 |
| 8 | Indices and tables | 55 |
| | Python Module Index | 57 |
| | Index | 59 |

INTRODUCTION

IDP-Z3 is a software collection implementing the Knowledge Base paradigm using the FO(.) language. FO(.) is First Order logic, extended with definitions, types, arithmetic, aggregates and intensional objects.

In the Knowledge Base paradigm, the knowledge about a particular problem domain is encoded using a declarative language, and later used to solve particular problems by applying the appropriate type of reasoning, or “inference”. The inferences include:

- model checking: does a particular solution satisfy the laws in the knowledge base ?
- model search: extend a partial solution into a full solution
- model propagation: find the facts that are common to all solutions that extend a partial one

The *IDP-Z3 engine* enables the creation of these solutions:

- the *Interactive Consultant*, which allow a knowledge expert to enter knowledge about a particular problem domain, and an end user to interactively find solutions for particular problem instances;
- *a program* with a command line interface to compute inferences on a knowledge base;
- a *web-based Interactive Development Environment (IDE)* to create Knowledge bases.

Warning: You may want to verify that you are seeing the documentation relevant for the version of IDP-Z3 you are using. On [readthedocs](#), you can see the version under the title (top left corner), and you can change it using the listbox at the bottom left corner.

1.1 Installation using poetry

Poetry is a package manager for python.

- Install python3 on your machine
- Install poetry
 - after that, logout and login if requested, to update \$PATH
- Use git to clone <https://gitlab.com/krr/IDP-Z3> to a directory on your machine
- Open a terminal in that directory
- If you have several versions of python3, and want to run on a particular one, e.g., 3.9:
 - run `poetry env use 3.9`
 - replace `python3` by `python3.9` in the commands below

- Run `poetry install`

To launch the Interactive Consultant web server:

- open a terminal in that directory and run `poetry run python3 main.py`

After that, you can open

- the Interactive Consultant at <http://127.0.0.1:5000>
- the web IDE at <http://127.0.0.1:5000/IDE>

1.2 Installation using pip

IDP-Z3 can be installed using the python package ecosystem.

- install `python 3`, with `pip3`, making sure that `python3` is in the `PATH`.
- use `git` to clone <https://gitlab.com/krr/IDP-Z3> to a directory on your machine
- (For Linux and MacOS) open a terminal in that directory and run the following commands.

```
python3 -m venv .
source bin/activate
python3 -m pip install -r requirements.txt
```

- (For Windows) open a terminal in that directory and run the following commands.

```
python3 -m venv .
.\Scripts\activate
python3 -m pip install -r requirements.txt
```

To launch the web server on Linux/MacOS, run

```
source bin/activate
python3 main.py
```

On Windows, the commands are:

```
.\Scripts\activate
python3 main.py
```

After that, you can open

- the Interactive Consultant at <http://127.0.0.1:5000>
- the web IDE at <http://127.0.0.1:5000/IDE>

1.3 Installation of `idp_engine` module

The `idp_engine` module is available for installation through the official Python package repository. This comes with a command line program, `idp_engine` that functions as described in *Command Line Interface*.

To install the module via poetry, the following commands can be used to add the module, and then install it.

```
poetry add idp_engine
poetry install
```

Installing the module via pip can be done as such:

```
pip3 install idp_engine
```


THE IDP LANGUAGE

2.1 Overview

The IDP language is used to create knowledge bases. An IDP source file is made of the following blocks of code:

vocabulary specify the types, predicates, functions and constants used to describe the problem domain.

theory specify the definitions and constraints satisfied by any solutions.

structure (optional) specify the interpretation of some predicates, functions and constants.

display (optional) configure the user interface of the *Interactive Consultant*.

main (optional) executable procedure in the context of the knowledge base

The basic skeleton of an IDP knowledge base for the Interactive Consultant is as follows:

```
vocabulary {
    // here comes the specification of the vocabulary
}

theory {
    // here comes the definitions and constraints
}

structure {
    // here comes the interpretation of some symbols
}

display {
    // here comes the configuration of the user interface
}
```

Everything between // and the end of the line is a comment.

2.2 Shebang

New in version 0.5.5

The first line of an IDP source file may be a [shebang](#) line, specifying the version of IDP-Z3 to be used. When a version is specified, the Interactive Consultant and Web IDE will be redirected to a server on the web running that version. The list of versions is available [here](#). (The IDP-Z3 executable ignores the shebang.)

Example: `#! IDP-Z3 0.5.4`

2.3 Vocabulary

```
vocabulary V {
  // here comes the vocabulary named V
}
```

The *vocabulary* block specifies the types, predicates, functions and constants used to describe the problem domain. If the name is omitted, the vocabulary is named V.

Each declaration goes on a new line (or are space separated). Symbols begins with a word character excluding digits, followed by word characters. Word characters include alphabetic characters, digits, `_`, and unicode characters that can occur in words. Symbols can also be string literals delimited by `'`, e.g., `'blue planet'`.

2.3.1 Types

IDP-Z3 supports built-in and custom types.

The built-in types are: `, , , Date`, and `Symbol`. The equivalent ASCII symbols are `Bool`, `Int`, and `Real`.

Boolean literals are `true` and `false`. Number literals follow Python's conventions. Date literals follow ISO 8601 conventions, prefixed with `#` (`#yyyy-mm-dd`). `#TODAY` is also a `Date` literal.

The type `Symbol` has one constructor for each symbol (i.e., function, predicate or constant) declared in the vocabulary. The constructors are the names of the symbol, prefixed with ```

Custom types are declared using the keyword `type`, e.g., `type color`. Their name should be singular and capitalized, by convention.

Their extension can be defined in a *structure*, or directly in the vocabulary, by specifying:

- a list of (ranges of) numeric literals, e.g., `type someNumbers := {0,1,2}` or `type byte := {0..255}`
- a list of (ranges of) dates, e.g., `type dates := {#2021-01-01, #2022-01-01}` or `type dates := {#2021-01-01 .. #2022-01-01}`
- a list of nullary constructors, e.g., `type Color := {Red, Blue, Green}`
- a list of n-ary constructors; in that case, the enumeration must be preceded by `constructed from`, e.g., `type Color2 := constructed from {Red, Blue, Green, RGB(R: Byte, G: Byte, B: Byte)}`

In the above example, the constructors of ``Color` are `: Red, Blue, Green`.

The constructors of ``Color2` are `: Red, Blue, Green` and `RGB`. Each constructor have an associated function (e.g., `is_Red`, or `is_RGB`) to test if a `Color2` term was created with that constructor. The `RGB` constructor takes 3 arguments of type `Byte`. `R`, `G` and `B` are accessor functions: when given a `Color2` term constructed with `RGB`, they return the associated `Byte`. (When given a `Color2` not constructed with `RGB`, they may raise an error)

2.3.2 Functions

The functions with name `MyFunc1`, `MyFunc2`, input types `T1`, `T2`, `T3` and output type `T`, are declared by:

```
myFunc1, myFunc2 : T1 T2 T3 → T
```

Their name should not start with a capital letter, by convention. The ASCII equivalent of `is *`, and of `→` is `->`.

IDP-Z3 does not support partial functions.

2.3.3 Built-in functions

The following functions are built-in:

- `abs: Int → Int` (or `abs: Float → Float`) yields the absolute value of an integer (or float) expression;
- `arity: Symbol → Symbol` yields the arity of a symbol;
- `input_domain : Symbol → Symbol` yields the n-th input-domain of a symbol;
- `output_domain: Symbol → Symbol` yields the output domain of a symbol.

2.3.4 Predicates

The predicates with name `myPred1`, `myPred2` and argument types `T1`, `T2`, `T3` are declared by:

```
myPred1, myPred2 : T1 T2 T3 →
```

Their name should not start with a capital letter, by convention. The ASCII equivalent of `→` is `->`, and of `is Bool`.

2.3.5 Propositions and Constants

A proposition is a predicate of arity 0; a constant is a function of arity 0.

```
MyProposition : () →
MyConstant: () → Int
```

2.3.6 Include another vocabulary

A vocabulary `W` may include a previously defined vocabulary `V`:

```
vocabulary W {
  extern vocabulary V
  // here comes the vocabulary named V
}
```

2.4 Theory

```
theory T:V {
  // here comes the theory named T, on vocabulary named V
}
```

A *theory* is a set of constraints and definitions to be satisfied. If the names are omitted, the theory is named T, for vocabulary V.

Before explaining their syntax, we need to introduce the concept of term.

2.4.1 Mathematical expressions and Terms

A *term* is inductively defined as follows:

Numeric literal Numeric literals that follow the [Python conventions](#) are numerical terms of type `Int` or `Real`.

Constructor Each constructor of a *type* is a term having that type.

Variable a variable is a term. Its *type* is derived from the *quantifier expression* that declares it (see below).

Function application $F(t_1, t_2, \dots, t_n)$ is a term, when F is a *function* symbol of arity n , and t_1, t_2, \dots, t_n are terms. Each term must be of the appropriate *type*, as defined in the function declaration in the vocabulary. The resulting type of the function application is also defined in the function declaration. If the arity of F is 0, i.e., if F is a *constant*, then $F()$ is a term.

$\$(s)(t_1, t_2, \dots, t_n)$ is a term, when s is an expression of type `Symbol` that denotes a function of arity n , and t_1, t_2, \dots, t_n are terms.

Please note that there are built-in *functions* (see [Built-in functions](#)).

Negation $\neg t$ is a numerical term, when t is a numerical term.

Arithmetic $t_1 \ op \ t_2$ is a numerical term, when t_1, t_2 are two numerical terms, and $\ op$ is one of the following math operators `+`, `-`, `*` (or `*`), `/`, `^`, `%`. Mathematical operators can be chained as customary (e.g. $x+y+z$). The usual order of binding is used.

Parenthesis (t) is a term, when t is a term

Cardinality aggregate $\#\{v_1 \text{ in } \text{typeOfV}_1, \dots, v_n \text{ in } \text{typeOfV}_n : \ \ \ \ \}$ is a numerical term when $v_1 \ v_2 \ \dots \ v_n$ are variables, and $\ \ \ \ \$ is a *sentence* containing these variables.

The term denotes the number of tuples of distinct values for $v_1 \ v_2 \ \dots \ v_n$ which make $\ \ \ \ \$ true.

Arithmetic aggregate $\{v_1 \text{ in } \text{typeOfV}_1, \dots, v_n \text{ in } \text{typeOfV}_n : \ \ \ \ \ : \ t\}$ is a numerical term when $\ \ \ \ \$ is sum, $v_1 \ v_2 \ \dots \ v_n$ are variables, $\ \ \ \ \$ is a *sentence*, and t is a term.

The term $\text{sum}\{v \text{ in } T : (v) : \ t(v)\}$ denotes the sum of $t(v)$ for each distinct value of v which makes $\text{phi}(v)$ true.

(if .. then .. else ..) $(\text{if } t_1 \text{ then } t_2 \text{ else } t_3)$ is a term when t_1 is a sentence, t_2 and t_3 are terms of the same type.

2.4.2 Sentences and constraints

A *constraint* is a sentence followed by `..`. A *sentence* is inductively defined as follows:

true and false `true` and `false` are sentences.

Predicate application $P(t_1, t_2, \dots, t_n)$ is a sentence, when P is a *predicate* symbol of arity n , and t_1, t_2, \dots, t_n are terms. Each term must be of the appropriate *type*, as defined in the predicate declaration. If the arity of P is 0, i.e., if P is a proposition, then $P()$ is a sentence.

$\$(s)(t_1, t_2, \dots, t_n)$ is a sentence, when s is an expression of type `Symbol` that denotes a predicate of arity n , and t_1, t_2, \dots, t_n are terms.

Comparison $t_1 \text{ op } t_2$ is a sentence, when t_1, t_2 are two numerical terms and `op` is one of the following comparison operators `<, >, =, <=, >=` (or, using ascii characters: `<, >, =, <=, >=`). Comparison operators can be chained as customary.

Negation \neg is a sentence (or, using ascii characters: `~`) when is is a sentence.

Logic connectives $is_1 \text{ op } is_2$ is a sentence when is_1, is_2 are two sentences and `op` is one of the following logic connectives `and, or, not, implies, iff` (or using ascii characters: `|, \&, =>, <=, <=>` respectively). Logic connectives can be chained as customary.

Parenthesis (is) is a sentence when is is a sentence.

Enumeration An enumeration (e.g. `p := {1;2;3}`) is a sentence. Enumerations follow the syntax described in *structure*.

Quantified formulas *Quantified formulas* are sentences. They have one of the following forms, where v_1, \dots, v_n are variables, p, p_1, \dots, p_n are types or predicates, and is is a sentence involving those variables:

```
v_1, v_n: (v_1, v_n).
v_1, v_n p: (v_1, v_n).
(v_1, v_n) p: (v_1, v_n).
v_1 p_1, v_n p_n: (v_1, v_n).
```

Alternatively, the existential quantifier, `exists`, can be used. Ascii characters can also be used: `?, !`, respectively. For example, `! x, y in Int: f(x,y)=f(y,x)`.

A variable may only occur in the sentence of a quantifier declaring that variable. In the first form above, the type of each variable is inferred from their use in `is`.

When quantifying a formula of type `Symbol`, the expression must contain a “guard” to prevent arity or type error. A guard is a condition that can be resolved using the available enumerations. In the following example, `symmetric` must be defined by enumeration.

```
symmetric := {`edge}
s Symbol: symmetric(s) => (x, y : $(s)(x,y) $(s)(y,x)).
```

An alternative is to use the introspection functions `arity`, `input_domain`, `output_domain`:

```
s Symbol: arity(s)=2 input_domain(s,1)=input_domain(s,2)
(x $(input_domain(s,1)), y $(input_domain(s,2)) : $(s)(x,y) $(s)(y,x)).
```

“is (not) enumerated” $f(a,b)$ is enumerated and $f(a,b)$ is not enumerated are sentences, where f is a function defined by an enumeration and applied to arguments a and b . Its truth value reflects whether (a,b) is enumerated in f ’s enumeration. If the enumeration has a default value, every tuple of arguments is enumerated.

“(not in {1,2,3,4})” $f(\text{args})$ in enum and $f(\text{args})$ not in enum are sentences, where f is a function applied to arguments args and enum is an enumeration. This can also be written using Unicode: $f() \{1, 2, 3\}$ or $f() \{1, 2, 3\}$.

if .. then .. else .. if t_1 then t_2 else t_3 is a sentence when t_1, t_2 and t_3 are sentences.

2.4.3 Definitions

A *definition* defines concepts, i.e. *predicates* or *functions*, in terms of other concepts. If a predicate is inductively defined in terms of itself, the definition employs the *well-founded* semantics. A definition consists of a set of rules, enclosed by { and }.

Rules have one of the following forms:

```
v_1 T_1, v_n T_n: P(t_1, .., t_n) ← |phi|.
v_1 T_1, v_n T_n: F(t_1, .., t_n) = t ← |phi|.
```

where P is a *predicate* symbol, F is a *function* symbol, t, t_1, t_2, \dots, t_n are terms that may contain the variables $v_1 v_2 \dots v_n$ and ϕ is a formula that may contain these variables. $P(t_1, t_2, \dots, t_n)$ is called the *head* of the rule and ϕ the *body*. \leftarrow can be used instead of \leftarrow . If the body is `true`, the left arrow and body of the rule can be omitted.

2.5 Structure

```
structure S:V {
  // here comes the structure named S, for vocabulary named V
}
```

A *structure* specifies the interpretation of some *type*, *predicates* and *functions*, by enumeration. If the names are omitted, the structure is named S , for vocabulary V .

A structure is a set of statement of the form $\langle \text{symbol} \rangle := \langle \text{enumeration} \rangle$, e.g., $P := \{1..9\}$, where the enumeration can be:

for nullary predicates (propositions) `true` or `false`

for non-numeric types and unary predicates: a set of rigid terms (numbers, dates, identifiers, or constructors applied to rigid terms), e.g., `{red, blue, green}`.

for numeric types and unary predicates: a set of numeric literals and ranges, e.g., `{0, 1, 2}`, `{0..255}` or `{0..9, 90..99}`

for date types and unary predicates: a set of date literals and ranges, e.g., `{#2021-01-01, #2022-01-01}` or `{#2021-01-01 .. #2022-01-01}`

for types: a set of n -ary constructors, preceded by `constructed from`, e.g., `constructed from {Red, Blue, Green, RGB(R: Byte, G: Byte, B: Byte)}` (see more details in *types*)

for n -ary predicates: a set of tuples of rigid terms, e.g., `{(a, b), (a, c)}`.

for nullary functions: a rigid term, e.g. `5` or `#2021-01-01`, or `red` or `rgb(0, 0, 0)`

for n -ary functions: a set of tuples and their associated values, e.g., `{(1, 2) -> 3, (4, 5) -> 6}`

Additional notes:

- the enumeration for a predicate specifies the tuples that make the predicate true; any other tuple make it false.

- the enumeration for a function may be followed by `else <default>`, where `<default>` is a default value (a rigid term), i.e., a value for the non-enumerated tuples, if any.
- parenthesis around a tuple can be omitted when the arity is 1, e.g., `{1-2, 3->4}`
- a predicate may be enumerated using a CSV format, with one tuple per line, e.g., :

```
P := {
1 2
3 4
5 6
}
```

2.6 Main block

The *main block* consists of python-like statements to be executed by the *IDP-Z3 executable* or the Web IDE, in the context of the knowledge base. It takes the following form:

```
procedure main() {
    // here comes the python-like code to be executed
}
```

The vocabularies, theories and structures defined in other blocks of the IDP source file are available through variables of the same name.

The following functions are available:

model_check(theory, structure=None) Returns string `sat`, `unsat` or `unknown`, depending on whether the theory has a model expanding the structure. `theory` and `structure` can be lists, in which case their elements are merged. The structure is optional.

For example, `print(model_check(T, S))` will print `sat` if theory named `T` has a model expanding structure named `S`.

model_expand(theory, structure=None, max=10, complete=False) Returns a list of models of the theory that are expansion of the structure. `theory` and `structure` can be lists, in which case their elements are merged. The structure is optional. The result is limited to `max` models (10 by default), or unlimited if `max` is 0. The models can be asked to be complete or partial (i.e., in which “don’t care” terms are not specified).

For example, `print(model_expand(T, S))` will print (up to) 10 models of theory named `T` expanding structure named `S`.

model_propagate(theory, structure=None) Returns a list of assignments that are true in any expansion of the structure consistent with the theory. `theory` and `structure` can be lists, in which case their elements are merged. The structure is optional. Terms and symbols starting with ‘_’ are ignored.

For example, `print(model_propagate(T, S))` will print the assignments that are true in any expansion of the structure named `S` consistent with the theory named `T`.

decision_table(theories, structures=None, goal_string="", timeout=20, max_rows=50, first_hit=True)

Experimental. Returns the rows for a decision table that defines `goal_string`. `goal_string` must be a predicate application defined in the theory.

pretty_print(...) Prints its argument on stdout, in a readable form.

2.6.1 Problem class

The main block can also use instances of the `Problem` class. This is beneficial when several inferences must be made in a row (e.g., `Problem(T, S).propagate().simplify().formula()`). Instances of the `Problem` class represent a collection of theory and structure blocks. The class has the following methods:

`__init__(self, *blocks, extended=False)` Creates an instance of `Problem` for the list of blocks, e.g., `Problem(T, S)`.

Use `extended=True` when the truth value of inequalities and quantified formula is of interest (e.g. for the Interactive Consultant).

`add(self, *blocks)` Adds a list of theory or structure blocks to the problem.

`assert_(self, code: str, value: Any)` Asserts that an expression has a value, e.g. `problem.assert_("p()", True)`.

`copy(self)` Returns an independent copy of a problem.

`formula(self)` Returns a Z3 object representing the logic formula equivalent to the problem. This object can be converted to a string using `str()`.

`expand(self, max=10, complete=False)` Returns a list of models of the theory that are expansion of the known assignments. The result is limited to `max` models (10 by default), or unlimited if `max` is 0. The models can be asked to be complete or partial (i.e., in which “don’t care” terms are not specified).

`optimize(self, term, minimize=True, complete=False)` Returns the problem with its `assignments` property updated with values such that the term is minimized (or maximized if `minimize` is `False`) `term` is a string (e.g. `"Length(1)"`). The models can be asked to be complete or partial (i.e., in which “don’t care” terms are not specified).

`symbolic_propagate(self)` Returns the problem with its `assignments` property updated with direct consequences of the constraints of the problem. This propagation is less complete than `propagate()`.

`propagate(self)` Returns the problem with its `assignments` property updated with values for all terms and atoms that have the same value in every model (i.e., satisfying structure of the problem). Terms and propositions starting with ‘_’ are ignored.

`get_range(self, term:str)` Returns a list of the possible values of the term (as strings).

`explain(self, consequence)` Returns the facts and laws to explain a consequence in the Problem.

The string `consequence` must be a key in the `assignments` property of the Problem. The facts are a list of Assignment, and the laws are a list of Expression.

`simplify(self)` Returns a simpler copy of the problem, with a simplified formula obtained by substituting terms and atoms by their known values.

`decision_table(self, goal_string="", timeout=20, max_rows=50, first_hit=True)` Experimental. Returns the rows for a decision table that defines `goal_string`. `goal_string` must be a predicate application defined in the theory. The problem must be created with `extended=True`.

`duration(msg: str)` Returns the processing time since the last call to `duration()`, or since the beginning of execution, followed by the `msg` (possibly an f-string)

2.7 Differences with IDP3

Here are the main differences with IDP3, listed for migration purposes:

min/max aggregates IDP-Z3 does not support these aggregates (yet). See [IEP 05](#)

Infinite domains IDP-Z3 supports infinite domains: `Int`, `Real`. However, quantifications over infinite domains is discouraged.

if .. then .. else .. IDP-Z3 supports *if.. then .. else ..* terms and sentences.

LTC IDP-Z3 does not support LTC vocabularies.

Namespaces IDP-Z3 does not support namespaces.

Partial functions IDP-Z3 does not support partial functions. The handling of division by 0 may differ. See [IEP 07](#)

Programming API IDP3 procedures are written in Lua, IDP-Z3 procedures are written in Python-like language.

Qualified quantifications IDP-Z3 does not support qualified quantifications, e.g. `!2 x[color]: p(x) ..` (p. 11 of the IDP3 manual).

Structure IDP-Z3 does not support uncertain interpretations (p.17 of IDP3 manual). Function enumerations must have an `else` part. (see also [IEP 04](#))

Type IDP-Z3 does not support type hierarchies.

To improve performance, do not quantify over the value of a function. Use `p(f(x))` instead of `?y: f(x)=y & p(y)`.

2.8 Syntax summary

The following code illustrates the syntax of IDP-Z3. `T` denotes a type, `c` a constructor, `p` a proposition or predicate, `f` a constant or function. The equivalent ASCII-only encoding is shown on the right.

```
vocabulary V {
  type T
  type T := {c1, c2, c3}
  type T := constructed from {c1, c2(T1, f:T2)}
  type T := {1,2,3}
  type T := {1..3}
  // built-in types: , , , Date, Symbol Bool, Int, Real, Date, Symbol

  p : () →
  p1, p2 : T1 T2 →
  f: T → T
  f1, f2: T → T

  p: () -> Bool
  p1, p2: T1*T2 -> Bool
  f: T -> T
  f1, f2: T -> T

  [this is the intended meaning of p]
  p : () →

  extern vocabulary W
}

theory T:V {
  (¬p1()p2() p3() p4() p5()) p6(). (¬p1()&p2() | p3() => p4() <=> p5()) <= p6().
  p(f1(f2())) .
  f1() < f2() f3() = f4() f5() > f6(). f1() < f2() =< f3() = f4() >= f5() > f6().
}
```

(continues on next page)

(continued from previous page)

```

f() c.                                f() ~= c.
x,y T: p(x,y).                        !x,y in T: p(x,y).
x p, (y,z) q: q(x,x) p(y) p(z).      !x in p, (y,z) in q: q(x,x) | p(y) | p(z).
x Symbol: arity(x)=0 $(x)().          ?x in Symbol: arity(x)=0 & $(x)().
x $(input_domain(`p,1)): p(x).        ?x in $(input_domain(`p,1)): p(x).
x: p(x).                               ?x: p(x).

f() in {1,2,3}.
f() = #{xT: p(x)}.                    f() = #{x in T: p(x)}.
f() = sum{xT: p(x): f(x)}.            f() = sum{x in T: p(x): f(x)}.
if p1() then p2() else p3().
f1() = if p() then f2() else f3().

p := {1,2,3}
p(#2020-01-01) is enumerated.
p(#TODAY) is not enumerated.

{ p(1).
  xT: p1(x) ← p2(x).                  !x in T: p1(x) <- p2(x).
  f(1)=1.
  x: f(x)=1 ← p(x).                  !x: f(x)=1 <- p(x).
}

[this is the intended meaning of the rule]
(p()).
}

structure S:V {
  p := false
  p := {1,2,3}
  p := {0..9, 100}
  p := {#2021-01-01}
  p := {(1,2), (3,4)}
  p := {
    1 2
    3 4
  }

  f := 1
  f := {→1}
  f := {1→1, 2→2}
  f := {(1,2)→3} else 2
}

f := {-> 1}
f := {1->1, 2->2}
f := {(1,2)->3} else 2

display {
  expand(`p).
  hide(`p).
  view() = expanded.
  relevant(`p1, `p2).
  goal(`p).
  optionalPropagation.
}

procedure main() {
  pretty_print(model_check      (T,S))
  pretty_print(model_expand    (T,S))
}

```

(continues on next page)

(continued from previous page)

```
pretty_print(model_propagate(T,S))  
}
```

See also the *Built-in functions*.

PYTHON API

The core of the IDP-Z3 software is a Python component [available on Pypi](#). The following code illustrates how to invoke it.

```
from idp_engine import IDP, model_expand
kb = IDP.from_file("path/to/file.idp")
T, S = kb.get_blocks("T, S")
for model in model_expand(T,S):
    print(model)
```

Besides the methods and class available in the *main block*, `idp_engine` exposes the `IDP` class, described below.

3.1 IDP class

The `IDP` class exposes the following methods:

from_file(file_path: str) This class method parses the *IDP source code* in the file located at `file_path`.

from_str(code: str) This class method parses the *IDP source code* in the `code` string.

parse(file_or_string) DEPRECATED: This class method parses the *IDP source code* in the file or string.

get_blocks(names) This instance method returns the list of blocks whose names are given in a comma-separated string.

execute() This instance methods executes the *main()* procedure block in the IDP source file.

COMMAND LINE INTERFACE

IDP-Z3 can be run through a Command Line Interface.

If you have downloaded IDP-Z3 from the GitLab repo, you may run the CLI using poetry (see [Installation](#)):

```
poetry run python3 idp-engine.py path/to/file.idp
```

where *path/to/file.idp* is the path to the file containing the IDP source file to be run. This file must contain a *main block*.

Alternatively, if you installed it via pip, you can run it with the following command:

```
idp-engine path/to/file.idp
```

The usage of the CLI is as follows:

```
usage: idp-engine.py [-h] [-o OUTPUT] [--full-formula] [--no-timing] FILE

IDP-Z3

positional arguments:
  FILE                path to the .idp file

optional arguments:
  -h, --help          show this help message and exit
  -o OUTPUT, --output OUTPUT
                    name of the output file
  --full-formula      show the full formula
  --no-timing         don't display timing information
```


INTERACTIVE CONSULTANT

The Interactive Consultant tool enables experts to digitize their knowledge of a specific problem domain. With the resulting knowledge base, an online interface is automatically created that serves as a web tool supporting end users to find solutions for specific problems within that knowledge domain.

The tool uses source code in the IDP-Z3 language as input. However, there are some specific changes and additions when using IDP-Z3 in the Interactive Consultant, which are explained further in this chapter.

5.1 Display

The *display block* configures the user interface of the *Interactive Consultant*. It consists of a set of *display facts*, i.e., *predicate* and *function applications* terminated by `..`

The following predicates and functions are available:

expand `expand(s1, .., sn)` specifies that *symbols* `s1, .., sn` are shown expanded, i.e., that all sub-sentences of the theory where they occur are shown on the screen.

For example, `expand(`Length) .` will force the Interactive Consultant to show all sub-sentences containing *Length*.

hide `hide(s1, .., sn)` specifies that symbols `s1, .., sn` are not shown on the screen.

For example, `hide(`Length) .` will force the Interactive Consultant to not display the box containing *Length* information.

view() `view() = normal.` (default) specifies that symbols are displayed in normal mode.

`view() = expanded.` specifies that symbols are displayed *expanded*.

relevant `relevant(s1, .., sn)` specifies that symbols `s1, .., sn` are relevant, i.e. that they should never be greyed out.

Irrelevant symbols and sub-sentences, i.e. symbols whose interpretation do not constrain the interpretation of the relevant symbols, are greyed out by the Interactive Consultant.

goal `goal(s)` specifies that symbols `s` is a goal, i.e. that it is relevant and shown expanded.

moveSymbols When the *display block* contains `moveSymbols()`, the Interactive Consultant is allowed to change the layout of symbols on the screen, so that relevant symbols come first.

By default, the symbols do not move.

optionalPropagation When the *display block* contains `optionalPropagation()`, a toggle button is shown next to the menu to allow toggling immediate propagation on and off.

By default, this button is not present.

manualPropagation When `manualPropagation()` is present in the *display block*, automatic propagation is disabled in the interface. Instead, a button is added to the menu that computes propagation when clicked.

optionalRelevance When the *display block* contains `optionalRelevance()`, a toggle button is shown next to the menu to allow toggling immediate computation of relevance on and off.

By default, this button is not present.

manualRelevance When `manualRelevance()` is present in the *display block*, automatic computation of relevant questions is disabled in the interface. Instead, a menu option is available in the “Reasoning” menu that computes relevance when selected.

unit `unit('unitstr', s1, ..., sn)` specifies the unit of one or more symbols. This unit will then show up in the symbol’s header in the Interactive Consultant. `unitstr` may not be a symbol declared in the vocabulary.

For example: `unit('m', length, perimeter)`.

heading Experimental: this feature is likely to change in the future.

`heading('label', `p1, ..., `pn)` will force the display of the ``p1, ..., `pn` symbols under a heading called `label`. `label` may not be a symbol declared in the vocabulary.

5.2 Vocabulary annotations

To improve the display of functions and predicates in the *Interactive Consultant*, they can be annotated with their intended meaning, a short comment, or a long comment. These annotations are enclosed in `[and]`, and come before the symbol declaration.

Intended meaning `[this is a text]` specifies the intended meaning of the symbol. This text is shown in the header of the symbol’s box.

Short info `[short:this is a short comment]` specifies the short comment of the symbol. This comment is shown when the mouse is over the info icon in the header of the symbol’s box.

Long info `[long:this is a long comment]` specifies the long comment of the symbol. This comment is shown when the user clicks the info icon in the header of the symbol’s box.

5.3 Environment

Often, some elements of a problem instance are under the control of the user (possibly indirectly), while others are not.

To capture this difference, the IDP language allows the creation of 2 vocabularies and 2 theories. The first one is called ‘environment’, the second ‘decision’. Hence, a more advanced skeleton of an IDP knowledge base is:

```
vocabulary environment {
  // here comes the specification of the vocabulary to describe the environment
}

vocabulary decision {
  extern vocabulary environment
  // here comes the specification of the vocabulary to describe the decisions and
  ↳their consequences
}

theory environment:environment {
```

(continues on next page)

(continued from previous page)

```
// here comes the definitions and constraints satisfied by any environment,
↳possibly faced by the user
}

theory decision:decision {
  // here comes the definitions and constraints to be satisfied by any solution
}

structure environment:environment {
  // here comes the interpretation of some environmental symbols
}

structure decision:decision {
  // here comes the interpretation of some decision symbols
}

display {
  // here comes the configuration of the user interface
}
```

5.4 Default Structure

The *default structure* functions similarly to a normal *Structure*, in the sense that it can be used to set values of symbols. However, these values are set as if they were given by the user: they are shown in the interface as selected values. The symbols can still be assigned different values, or they can be unset.

In this way, this type of structure is used to form a *default* set of values for symbols. Such a structure is given the name 'default', to denote that it specifies default values. The syntax of the block remains the same.

```
structure default {
  // here comes the structure
}
```


APPENDIX: IDP-Z3 DEVELOPER REFERENCE

Note: The contents of this reference are intended for people who want to further develop IDP-Z3.

Note: Despite our best efforts, this documentation may not be complete and up-to-date.

The components of IDP-Z3 are shown below.

- [webIDE](#) client: browser-based application to edit and run IDP-Z3 programs
- [Interactive Consultant](#) client: browser-based user-friendly decision support application
- [Read_the_docs](#) : online documentation
- [Homepage](#)
- IDP-Z3 server: web server for both web applications
- IDP-Z3 command line interface
- IDP-Z3 engine: performs reasoning on IDP-Z3 theories
- [Z3](#): SMT solver developed by Microsoft

The [source code](#) of IDP-Z3 is publicly available under the GNU LGPL v3 license. You may want to check the [Development and deployment guide](#).

6.1 Architecture

This document presents the technical architecture of IDP-Z3.

Essentially, the IDP-Z3 components translate the requested inferences on the knowledge base into satisfiability problems that Z3 can solve.

6.1.1 Web clients

The repository for the web clients is in a [separate GitLab repository](#).

The clients are written in [Typescript](#), using the [Angular](#) framework (version 7.1), and the [primeNG](#) library of widgets. It uses the [Monaco editor](#). The interactions with the server are controlled by [idp.service.ts](#). The [AppSettings file](#) contains important settings, such as the address of the IDP-Z3 sample theories.

The web clients are sent to the browser by the IDP-Z3 server as static files. The static files are generated by the `/IDP-Z3/deploy.py` script as part of the deployment, and saved in the `/IDP-Z3/idp_server/static` folder.

See the Appendix of [Development and deployment guide](#) on the wiki for a discussion on how to set-up your environment to develop web clients.

The `/docs/zettlr/REST.md` file describes the format of the data exchanged between the web client and the server. The exchange of data while using web clients can be visualised in the developer mode of most browsers (Chrome, Mozilla, ...).

The web clients could be packaged into an executable using [nativefier](#).

6.1.2 Read The Docs, Homepage

The [online documentation](#) and [Homepage](#) are written in [ReStructuredText](#), generated using [sphinx](#) and hosted on [readthedocs.org](#) and [GitLab Pages](#) respectively. The contents is in the `/docs` and `/homepage` folders of IDP-Z3.

We use the following sphinx extensions: [Mermaid \(diagrams\)](#), and [Markdown](#).

6.1.3 IDP-Z3 server

The code for the IDP-Z3 server is in the `/idp_server` folder.

The IDP-Z3 server is written in python 3.8, using the [Flask framework](#). Pages are served by `/idp_server/rest.py`. Static files are served from the `/idp_server/static` directory, including the compiled version of the client software.

At start-up, and every time the idp code is changed on the client, the idp code is sent to the `/meta` URL by the client. The server responds with the list of symbols to be displayed. A subsequent call (`/eval`) returns the questions to be displayed. After that, when the user clicks on a GUI element, information is sent to the `/eval` URL, and the server responds as necessary.

The information given by the user is combined with the idp code (in [State.py](#)), and, using adequate inferences, the questions are put in these categories with their associated value (if any):

- given: given by the user
- universal: always true (or false), per idp code
- consequences: consequences of user's input according to theory
- irrelevant: made irrelevant by user's input
- unknown

The IDP-Z3 server implements custom inferences such as the computation of relevance ([Inferences.py](#)), and the handling of environmental vs. decision variables.

API endpoints

The IDP-Z3 server exposes multiple API endpoints, which are used to communicate information between the interface and server.

`/run`

POST: Runs an IDP program containing a main block. The program is be executed by the IDP-Z3 directly, and the output is returned. This endpoint is e.g. used to execute the code in the IDP webIDE.

Arguments:

- **code:** IDP code, containing a main block.

Returns:

- A string, containing the output of the IDP-Z3 engine after executing the program.

`/meta`

POST: generate the metaJSON for an IDP program. In the IC, this metaJSON is among others used to correctly lay out the different symbol tiles and to generate extra expanded symbols.

Arguments:

- **code:** IDP code, with or without main block.

Returns:

- **title:** the title that the IC should have.
- **symbols:** contains information on each symbol used in the IDP program. This information includes symbol name, type, view, ...
- **optionalPropagation:** a bool representing if a propagation toggle should be shown in the interface.
- **manualPropagation:** a bool representing if propagation should be manual via a button.
- **optionalRelevance:** a bool representing if a relevance toggle should be shown in the interface.
- **manualRelevance:** a bool representing if relevance computation should be manual via a button.
- **propagated:** contains the information on all the (expanded) symbols.

`/eval`

POST: execute one of IDP-Z3's inference methods.

Arguments:

- **method:** string containing the method to execute. Supported methods are: *propagate*, *get_range*, *modelexpand*, *explain*, *minimize*, and *abstract*.
- **code:** the IDP code.
- **active:** the active assignments, already input in the interface.
- **previous_active:** the same as the above, sans the last added assignment.
- **symbol:** the name of a symbol, only used for *minimize* or *explain*.

- **value**: a value, only used for *explain*.
- **field**: the applied symbol for which a range must be determined, only for *get_range*.
- **minimize**: *true* for minimization, *false* for maximization.

Returns:

- **Global**: the global information of the current state of the IC.
- A field for every symbol that appears in the IDP program, containing all its information.

6.1.4 IDP-Z3 engine

The code for the IDP-Z3 engine and IDP-Z3-CLI is in the `/idp_engine` folder. The IDP-Z3 engine exposes an API implemented by `Run.py` and `Problem.py`.

Translating knowledge inferences into satisfiability problems that Z3 can solve involves these steps:

1. parsing the idp code and the info entered by the user,
2. converting it to the Z3 format,
3. calling the appropriate method,
4. formatting the response.

The IDP-Z3 code is parsed into an **abstract syntax tree (AST)** using the `textx` package, according to [this grammar](#). There is one python class per type of AST nodes (see `Parse.py` and `Expression.py`)

The conversion to the Z3 format is performed by the following passes over the AST generated by the parser:

1. annotate the nodes by resolving names, and computing some derived information (e.g. type) (`annotate()`)
2. expand quantifiers in the theory, as far as possible. (`interpret()`)
3. when a structure is given, use the interpretation (`interpret()`), i.e.:
 - a) expand quantifiers based on the structure (grounding); perform type inference as necessary;
 - b) simplify the theory using the data in the structure and the laws of logic;
 - c) instantiate the definitions for every calls of the defined symbols (recursively)
4. convert to Z3, adding the type constraints not enforced by Z3 (`.translate()`)

The graph of calls is outlined in `/docs/zettlr/Call_graph.md`.

The code is organised by steps, not by classes: for example, all methods to annotate an expression by another are grouped in `Annotate.py`. We use **monkey-patching** to attach methods to the classes declared in another module.

Important classes of the IDP-Z3 engine are: `Expression`, `Assignment`, `Problem`.

`Substitute()` modifies the AST “in place”. Because the results of step 1-2 are cached, steps 4-7 are done after copying the AST (`custom_copy()`).

6.1.5 Z3

See [this tutorial](#) for an introduction to Z3 (or [this guide](#)).

You may also want to refer to the [Z3py](#) reference.

6.1.6 Appendix: Dependencies and Licences

The IDP-Z3 tools are published under the [GNU LGPL v3 license](#).

The server software uses the following components (see [requirements.txt](#)):

- Z3: MIT license
- Z3-solver: MIT license
- Flask: BSD License (BSD-3-Clause)
- flask_restful : BSD license
- flask_cors : MIT license
- pycallgraph2 : GNU GPLv2
- gunicorn : MIT license
- textx: MIT license

The client-side software uses the following components:

- Angular: MIT-style license
- PrimeNg: MIT license
- ngx-monaco-editor: MIT license
- packery: GPL-3.0
- primeicons: MIT
- isotope-layout: GNU GPL-3.0
- isotope-packery: MIT
- core-js: MIT
- dev: None
- git-describe: MIT
- rxjs: Apache 2.0
- tslib: Apache 2.0
- zone.js: MIT

6.2 idp_engine module

6.2.1 idp_engine.Parse

Classes to parse an IDP-Z3 theory.

class `idp_engine.Parse.IDP` (***kwargs*)
 Bases: `idp_engine.Expression.ASTNode`

The class of AST nodes representing an IDP-Z3 program.

Parameters

- **code** (*str*) – source code of the IDP program
- **vocabularies** (*dict[str, Vocabulary]*) – list of vocabulary blocks, by name
- **theories** (*dict[str, Theory]*) – list of theory blocks, by name
- **structures** (*dict[str, Structure]*) – list of structure blocks, by name
- **procedures** (*dict[str, Procedure]*) – list of procedure blocks, by name
- **display** (*Display, Optional*) – display block, if any

classmethod `from_file` (*file: str*) → `idp_engine.Parse.IDP`
 parse an IDP program from file

Parameters **file** (*str*) – path to the source file

Returns the result of parsing the IDP program

Return type *IDP*

classmethod `from_str` (*code: str*) → `idp_engine.Parse.IDP`
 parse an IDP program

Parameters **code** (*str*) – source code to be parsed

Returns the result of parsing the IDP program

Return type *IDP*

classmethod `parse` (*file_or_string: str*) → `idp_engine.Parse.IDP`
 DEPRECATED: parse an IDP program

Parameters **file_or_string** (*str*) – path to the source file, or the source code itself

Returns the result of parsing the IDP program

Return type *IDP*

get_blocks (*blocks: List[str]*)

returns the AST nodes for the blocks whose names are given

Parameters **blocks** (*List[str]*) – list of names of the blocks to retrieve

Returns list of AST nodes

Return type List[Union[*Vocabulary, Theory, Structure, Procedure, Display*]]

execute ()

Execute the IDP program

```
class idp_engine.Parse.Vocabulary (**kwargs)
```

Bases: *idp_engine.Expression.ASTNode*

The class of AST nodes representing a vocabulary block.

```
add_voc_to_block (block)
```

adds the enumerations in a vocabulary to a theory or structure block

Parameters **block** (*Problem*) – the block to be updated

```
class idp_engine.Parse.Annotations (**kwargs)
```

Bases: *idp_engine.Expression.ASTNode*

```
class idp_engine.Parse.Extern (**kwargs)
```

Bases: *idp_engine.Expression.ASTNode*

```
class idp_engine.Parse.TypeDeclaration (**kwargs)
```

Bases: *idp_engine.Expression.ASTNode*

AST node to represent *type* *<symbol> := <enumeration>*

Parameters

- **name** (*string*) – name of the type
- **arity** (*int*) – the number of arguments
- **sorts** (*List[Symbol]*) – the types of the arguments
- **out** (*Symbol*) – the Boolean Symbol
- **type** (*string*) – Z3 type of an element of the type; same as *name*
- **constructors** (*[Constructor]*) – list of constructors in the enumeration
- **range** (*[Expression]*) – list of expressions of that type
- **interpretation** (*SymbolInterpretation*) – the symbol interpretation
- **map** (*Dict[string, Expression]*) – a mapping from code to Expression in range

```
class idp_engine.Parse.SymbolDeclaration (**kwargs)
```

Bases: *idp_engine.Expression.ASTNode*

The class of AST nodes representing an entry in the vocabulary, declaring one or more symbols. Multi-symbols declaration are replaced by single-symbol declarations before the *annotate()* stage.

annotations

the annotations given by the expert.

annotations['reading'] is the annotation giving the intended meaning of the expression (in English).

symbols

the symbols being defined, before expansion

Type [*Symbol*]

name

the identifier of the symbol, after expansion of the node

Type *string*

arity

the number of arguments

Type *int*

sorts

the types of the arguments

Type List[*Symbol*]

out

the type of the symbol

Type *Symbol*

type

name of the Z3 type of an instance of the symbol

Type string

domain

the list of possible tuples of arguments

Type List

instances

a mapping from the code of a symbol applied to a tuple of arguments to its parsed AST

Type Dict[string, *Expression*]

range

the list of possible values

Type List[*Expression*]

private

True if the symbol name starts with ‘_’ (for use in IC)

Type Bool

unit

the unit of the symbol, such as m (meters)

Type str

heading

the heading that the symbol should belong to

Type str

```
class idp_engine.Parse.Symbol (**kwargs)
  Bases: idp_engine.Expression.Expression
```

Represents a Symbol. Handles synonyms.

name

name of the symbol

Type string

```
class idp_engine.Parse.Theory (**kwargs)
  Bases: idp_engine.Expression.ASTNode
```

The class of AST nodes representing a theory block.

```
class idp_engine.Parse.Definition (**kwargs)
  Bases: idp_engine.Expression.ASTNode
```

The class of AST nodes representing an inductive definition. id (num): unique identifier for each definition

rules ([**Rule**): set of rules for the definition, e.g., !x: $p(x) <- q(x)$

canonicals (`dict[Declaration, list[Rule]]`): normalized rule for each defined symbol, e.g., $!p!l!: p(!p!l!) \leftarrow q(!p!l!)$

instantiables (`dict[Declaration], list[Expression]`): list of instantiable expressions for each symbol, e.g., $p(!p!l!) \Leftrightarrow q(!p!l!)$

clarks (`dict[Declaration, Transformed Rule]`): normalized rule for each defined symbol (used to be Clark completion) e.g., $!p!l!: p(!p!l!) \Leftrightarrow q(!p!l!)$

def_vars (`dict[String, dict[String, Variable]]`): Fresh variables for arguments and result

level_symbols (`dict[SymbolDeclaration, Symbol]`): map of recursively defined symbols to level mapping symbols

cache (`dict[SymbolDeclaration, str, Expression]`): cache of instantiation of the definition

`inst_def_level` (int): depth of recursion during instantiation

set_level_symbols ()

Calculates which symbols in the definition are recursively defined, creates a corresponding level mapping symbol, and stores these in `self.level_symbols`.

add_def_constraints (`instantiables, problem, result`)
result is updated with the constraints for this definition.

The *instantiables* (of the definition) are expanded in *problem*.

Parameters

- **instantiables** (`dict[SymbolDeclaration, list[Expression]]`) – the constraints without the quantification
- **problem** (`Problem`) – contains the structure for the expansion/interpretation of the constraints
- **result** (`dict[SymbolDeclaration, Definition, list[Expression]]`) – a mapping from (Symbol, Definition) to the list of constraints

get_instantiables (`for_explain=False`)

compute `Definition.instantiables`, with level-mapping if definition is inductive

Uses implications instead of equivalence if `for_explain` is True

Example: $\{ p() \leftarrow q(). p() \leftarrow r(). \}$ Result when not `for_explain`: $p() \Leftrightarrow q() \mid r()$ Result when `for_explain`: $p() \Leftarrow q(). p() \Leftarrow r(). p() \Rightarrow (q() \mid r()).$

Parameters for_explain (`Bool`) – Use implications instead of equivalence, for rule-specific explanations

interpret (`problem`)

updates `problem.def_constraints`, by expanding the definitions

Parameters problem (`Problem`) – contains the enumerations for the expansion; is updated with the expanded definitions

class `idp_engine.Parse.Rule` (`**kwargs`)

Bases: `idp_engine.Expression.ASTNode`

instantiate_definition (`new_args, theory`)

Create an instance of the definition for `new_args`, and interpret it for `theory`.

Parameters

- **new_args** (`[Expression]`) – tuple of arguments to be applied to the defined symbol

- **theory** (*Problem*) – the context for the interpretation

Returns a boolean expression

Return type *Expression*

rename_args (*new_vars*)

for Clark's completion input : '!v: f(args) <- body(args)' output: '!nv: f(nv) <- nv=args & body(args)'

class `idp_engine.Parse.Structure` (**kwargs)

Bases: `idp_engine.Expression.ASTNode`

The class of AST nodes representing an structure block.

annotate (*idp*)

Annotates the structure with the enumerations found in it. Every enumeration is converted into an assignment, which is added to *self.assignments*.

Parameters *idp* – a *Parse.IDP* object.

Returns None

class `idp_engine.Parse.Enumeration` (**kwargs)

Bases: `idp_engine.Expression.ASTNode`

Represents an enumeration of tuples of expressions. Used for predicates, or types without n-ary constructors.

tuples

OrderedSet of Tuple of Expression

Type `OrderedSet[Tuple]`

constructors

List of Constructor

Type List[*Constructor*], optional

contains (*args, function, arity=None, rank=0, tuples=None*)

returns an Expression that says whether Tuple args is in the enumeration

class `idp_engine.Parse.Tuple` (**kwargs)

Bases: `idp_engine.Expression.ASTNode`

class `idp_engine.Parse.Display` (**kwargs)

Bases: `idp_engine.Expression.ASTNode`

class `idp_engine.Parse.Procedure` (**kwargs)

Bases: `idp_engine.Expression.ASTNode`

6.2.2 idp_engine.Expression

(They are monkey-patched by other modules)

class `idp_engine.Expression.ASTNode`

Bases: object

superclass of all AST nodes

check (*condition, msg*)

raises an exception if *condition* is not True

Parameters

- **condition** (*Bool*) – condition to be satisfied

- `msg (str)` – error message

Raises `IDPZ3Error` – when *condition* is not met

`dedup_nodes (kwargs, arg_name)`

pops *arg_name* from *kwargs* as a list of named items and returns a mapping from name to items

Parameters

- `kwargs (Dict[str, ASTNode])` –
- `arg_name (str)` – name of the *kwargs* argument, e.g. “interpretations”

Returns mapping from *name* to AST nodes

Return type `Dict[str, ASTNode]`

Raises `AssertionError` – in case of duplicate name

class `idp_engine.Expression.Expression`

Bases: `idp_engine.Expression.ASTNode`

The abstract class of AST nodes representing (sub-)expressions.

code

Textual representation of the expression. Often used as a key.

It is generated from the sub-tree. Some tree transformations change it (e.g., instantiate), others don't.

Type `string`

sub_exprs

The children of the AST node.

The list may be reduced by simplification.

Type `List[Expression]`

type

The name of the type of the expression, e.g., `bool`.

Type `string`

co_constraint

A constraint attached to the node.

For example, the `co_constraint` of `square(length(top()))` is `square(length(top())) = length(top()) * length(top())` ., assuming `square` is appropriately defined.

The `co_constraint` of a defined symbol applied to arguments is the instantiation of the definition for those arguments. This is useful for definitions over infinite domains, as well as to compute relevant questions.

Type `Expression`, optional

simpler

A simpler, equivalent expression.

Equivalence is computed in the context of the theory and structure. Simplifying an expression is useful for efficiency and to compute relevant questions.

Type `Expression`, optional

value

A rigid term equivalent to the expression, obtained by transformation.

Equivalence is computed in the context of the theory and structure.

Type `Optional[Expression]`

annotations

The set of annotations given by the expert in the IDP source code.

`annotations['reading']` is the annotation giving the intended meaning of the expression (in English).

Type Dict[str, str]

original

The original expression, before propagation and simplification.

Type *Expression*

fresh_vars

The set of names of the variables in the expression.

Type Set(string)

is_type_constraint_for

name of the symbol for which the expression is a type constraint

Type string

copy()

create a deep copy (except for rigid terms and variables)

collect (*questions*, *all_=True*, *co_constraints=True*)

collects the questions in self.

questions is an OrderedSet of Expression Questions are the terms and the simplest sub-formula that can be evaluated. *collect* uses the simplified version of the expression.

all_=False : ignore expanded formulas and AppliedSymbol interpreted in a structure *co_constraints=False* : ignore *co_constraints*

default implementation for UnappliedSymbol, IfExpr, AUnary, Variable, Number_constant, Brackets

collect_symbols (*symbols=None*, *co_constraints=True*)

returns the list of symbol declarations in self, ignoring type constraints

returns Dict[name, Declaration]

collect_nested_symbols (*symbols*, *is_nested*)

returns the set of symbol declarations that occur (in)directly under an aggregate or some nested term, where *is_nested* is flipped to True the moment we reach such an expression

returns {SymbolDeclaration}

generate_constructors (*constructors: dict*)

fills the list *constructors* with all constructors belonging to open types.

co_constraints (*co_constraints*)

collects the constraints attached to AST nodes, e.g. instantiated definitions

co_constraints is an OrderedSet of Expression

is_assignment () → bool

Returns True if *self* assigns a rigid term to a rigid function application

Return type bool

update_exprs (*new_exprs*)

change *sub_exprs* and simplify, while keeping relevant info.

substitute (*e0, e1, assignments, tag=None*)

recursively substitute e0 by e1 in self (e0 is not a Variable)

if tag is present, updates assignments with symbolic propagation of co-constraints.

implementation for everything but AppliedSymbol, UnappliedSymbol and Fresh_variable

instantiate (*e0, e1, problem=None*)

Recursively substitute Variable in e0 by e1 in a copy of self.

Interpret appliedSymbols immediately if grounded (and not occurring in head of definition). Update fresh_vars.

instantiate1 (*e0, e1, problem=None*)

Recursively substitute Variable in e0 by e1 in self.

Interpret appliedSymbols immediately if grounded (and not occurring in head of definition). Update fresh_vars.

simplify_with (*assignments: idp_engine.Assignments.Assignments*) →
idp_engine.Expression.Expression
 simplify the expression using the assignments

symbolic_propagate (*assignments: Assignments, tag: Status, truth: Optional[idp_engine.Expression.Expression] = true*) *Op-*
 updates assignments with the consequences of *self=truth*.

The consequences are obtained by symbolic processing (no calls to Z3).

Parameters

- **assignments** (*Assignments*) – The set of assignments to update.
- **truth** (*Expression, optional*) – The truth value of the expression *self*. Defaults to TRUE.

propagate1 (*assignments, tag, truth*)

returns the list of symbolic_propagate of self, ignoring value and simpler

translate (*problem: Problem, vars={}*) → *z3.z3.ExprRef*

Converts the syntax tree to a Z3 expression, using .value and .simpler if present

Parameters

- **problem** (*Problem*) – holds the context for the translation (e.g. a cache of translations).
- **vars** (*dict[id, ExprRef], optional*) – mapping from Variable’s id to Z3 translation. Filled in by AQuantifier. Defaults to {}.

Returns Z3 expression

Return type ExprRef

as_set_condition () → *Tuple[Optional[AppliedSymbol], Optional[bool], Optional[Enumeration]]*

Returns an equivalent expression of the type “x in y”, or None

Returns meaning “expr is (not) in enumeration”

Return type *Tuple[Optional[AppliedSymbol], Optional[bool], Optional[Enumeration]]*

split_equivalences ()

Returns an equivalent expression where equivalences are replaced by implications

Returns Expression

add_level_mapping (*level_symbols, head, pos_justification, polarity*)

Returns an expression where level mapping atoms (e.g., `lvl_p > lvl_q`) are added to atoms containing recursive symbols.

Parameters

- **level_symbols** (-) – the level mapping symbols as well as their corresponding recursive symbols
- **head** (-) – head of the rule we are adding level mapping symbols to.
- **pos_justification** (-) – whether we are adding symbols to the direct positive justification (e.g., head => body) or direct negative justification (e.g., body => head) part of the rule.
- **polarity** (-) – whether the current expression occurs under negation.

Returns Expression

annotate (*voc*, *q_vars*)
annotate tree after parsing

annotated1 ()
annotations that are common to `__init__` and `make()`

interpret (*problem*) → *idp_engine.Expression.Expression*
uses information in the problem and its vocabulary to: - expand quantifiers in the expression - simplify the expression using known assignments and enumerations - instantiate definitions

Parameters **problem** (*Problem*) – the Problem to apply

Returns the resulting expression

Return type *Expression*

class `idp_engine.Expression.Constructor` (***kwargs*)
Bases: *idp_engine.Expression.ASTNode*

Constructor declaration

name
name of the constructor

Type string

sorts
types of the arguments of the constructor

Type List[*Symbol*]

type
name of the type that contains this constructor

Type string

arity
number of arguments of the constructor

Type Int

tester
function to test if the constructor

Type *SymbolDeclaration*

has been applied to some arguments

Type e.g., `is_rgb`

symbol

only for Symbol constructors

Type *Symbol*

class `idp_engine.Expression.IfExpr` (**kwargs)

Bases: `idp_engine.Expression.Expression`

collect_nested_symbols (*symbols, is_nested*)

returns the set of symbol declarations that occur (in)directly under an aggregate or some nested term, where `is_nested` is flipped to `True` the moment we reach such an expression

returns {SymbolDeclaration}

translate1 (*problem: Problem, vars={}*) → `z3.z3.ExprRef`

Converts the syntax tree to a Z3 expression, ignoring `.value` and `.simpler`

Parameters

- **problem** (`Problem`) – holds the context for the translation (e.g. a cache of translations).
- **vars** (*dict[id, ExprRef], optional*) – mapping from Variable's id to Z3 translation. Filled in by `AQuantifier`. Defaults to {}.

Returns Z3 expression

Return type `ExprRef`

class `idp_engine.Expression.Quantee` (**kwargs)

Bases: `idp_engine.Expression.Expression`

represents the description of quantification, e.g., *x in T* or *(x,y) in P*

vars

the (tuples of) variables being quantified

Type `List[List[Variable]]`

sub_exprs

the type or predicate to quantify over

Type `List[SymbolExpr], Optional`

arity

the length of the tuple of variable

Type `int`

class `idp_engine.Expression.AQuantification` (**kwargs)

Bases: `idp_engine.Expression.Expression`

classmethod `make` (*q, quantees, f, annotations=None*)

make and annotate a quantified formula

copy ()

create a deep copy (except for rigid terms and variables)

collect (*questions, all_=True, co_constraints=True*)

collects the questions in self.

questions is an `OrderedSet` of `Expression Questions` are the terms and the simplest sub-formula that can be evaluated. *collect* uses the simplified version of the expression.

`all_=False` : ignore expanded formulas and AppliedSymbol interpreted in a structure `co_constraints=False`
: ignore `co_constraints`

default implementation for UnappliedSymbol, IfExpr, AUnary, Variable, Number_constant, Brackets

collect_symbols (*symbols=None, co_constraints=True*)
returns the list of symbol declarations in self, ignoring type constraints
returns Dict[name, Declaration]

interpret (*problem*)
apply information in the problem and its vocabulary
Parameters **problem** (Problem) – the problem to be applied
Returns the expanded quantifier expression
Return type *Expression*

class `idp_engine.Expression.Operator` (***kwargs*)
Bases: `idp_engine.Expression.Expression`

classmethod **make** (*ops, operands, annotations=None*)
creates a BinaryOp beware: cls must be specific for ops !

collect (*questions, all_=True, co_constraints=True*)
collects the questions in self.

questions is an OrderedSet of Expression Questions are the terms and the simplest sub-formula that can be evaluated. *collect* uses the simplified version of the expression.

`all_=False` : ignore expanded formulas and AppliedSymbol interpreted in a structure `co_constraints=False`
: ignore `co_constraints`

default implementation for UnappliedSymbol, IfExpr, AUnary, Variable, Number_constant, Brackets

collect_nested_symbols (*symbols, is_nested*)
returns the set of symbol declarations that occur (in)directly under an aggregate or some nested term, where *is_nested* is flipped to True the moment we reach such an expression
returns {SymbolDeclaration}

class `idp_engine.Expression.AImplication` (***kwargs*)
Bases: `idp_engine.Expression.Operator`

add_level_mapping (*level_symbols, head, pos_justification, polarity*)

Returns an expression where level mapping atoms (e.g., `lvl_p > lvl_q`) are added to atoms containing recursive symbols.

Parameters

- **level_symbols** (–) – the level mapping symbols as well as their corresponding recursive symbols
- **head** (–) – head of the rule we are adding level mapping symbols to.
- **pos_justification** (–) – whether we are adding symbols to the direct positive justification (e.g., `head => body`) or direct negative justification (e.g., `body => head`) part of the rule.
- **polarity** (–) – whether the current expression occurs under negation.

Returns Expression

```
class idp_engine.Expression.AEquivalence (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
  split_equivalences ()
```

```
    Returns an equivalent expression where equivalences are replaced by implications
```

```
    Returns Expression
```

```
class idp_engine.Expression.ARImplication (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
  add_level_mapping (level_symbols, head, pos_justification, polarity)
```

```
    Returns an expression where level mapping atoms (e.g.,  $lvl\_p > lvl\_q$ ) are added to atoms containing recursive symbols.
```

Parameters

- **level_symbols** (-) – the level mapping symbols as well as their corresponding recursive symbols
- **head** (-) – head of the rule we are adding level mapping symbols to.
- **pos_justification** (-) – whether we are adding symbols to the direct positive justification (e.g., $head \Rightarrow body$) or direct negative justification (e.g., $body \Rightarrow head$) part of the rule.
- **polarity** (-) – whether the current expression occurs under negation.

```
    Returns Expression
```

```
class idp_engine.Expression.ADisjunction (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
class idp_engine.Expression.AConjunction (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
class idp_engine.Expression.AComparison (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
  is_assignment ()
```

```
    Returns: bool: True if self assigns a rigid term to a rigid function application
```

```
class idp_engine.Expression.ASumMinus (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
class idp_engine.Expression.AMultDiv (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
class idp_engine.Expression.APower (**kwargs)
```

```
  Bases: idp_engine.Expression.Operator
```

```
class idp_engine.Expression.AUnary (**kwargs)
```

```
  Bases: idp_engine.Expression.Expression
```

```
  add_level_mapping (level_symbols, head, pos_justification, polarity)
```

```
    Returns an expression where level mapping atoms (e.g.,  $lvl\_p > lvl\_q$ ) are added to atoms containing recursive symbols.
```

Parameters

- **level_symbols** (-) – the level mapping symbols as well as their corresponding recursive symbols

- **head** (-) – head of the rule we are adding level mapping symbols to.
- **pos_justification** (-) – whether we are adding symbols to the direct positive justification (e.g., head => body) or direct negative justification (e.g., body => head) part of the rule.
- **polarity** (-) – whether the current expression occurs under negation.

Returns Expression

class `idp_engine.Expression.AAggregate` (**kwargs)

Bases: `idp_engine.Expression.Expression`

copy ()

create a deep copy (except for rigid terms and variables)

collect (*questions*, *all_=True*, *co_constraints=True*)

collects the questions in self.

questions is an OrderedSet of Expression Questions are the terms and the simplest sub-formula that can be evaluated. *collect* uses the simplified version of the expression.

all_=False : ignore expanded formulas and AppliedSymbol interpreted in a structure
co_constraints=False : ignore co_constraints

default implementation for UnappliedSymbol, IfExpr, AUnary, Variable, Number_constant, Brackets

collect_symbols (*symbols=None*, *co_constraints=True*)

returns the list of symbol declarations in self, ignoring type constraints

returns Dict[name, Declaration]

collect_nested_symbols (*symbols*, *is_nested*)

returns the set of symbol declarations that occur (in)directly under an aggregate or some nested term, where *is_nested* is flipped to True the moment we reach such an expression

returns {SymbolDeclaration}

class `idp_engine.Expression.AppliedSymbol` (**kwargs)

Bases: `idp_engine.Expression.Expression`

Represents a symbol applied to arguments

Parameters

- **symbol** (`Expression`) – the symbol to be applied to arguments
- **is_enumerated** (`string`) – ‘’ or ‘is enumerated’ or ‘is not enumerated’
- **is_enumeration** (`string`) – ‘’ or ‘in’ or ‘not in’
- **in_enumeration** (`Enumeration`) – the enumeration following ‘in’
- **decl** (`Declaration`) – the declaration of the symbol, if known
- **in_head** (`Bool`) – True if the AppliedSymbol occurs in the head of a rule

copy ()

create a deep copy (except for rigid terms and variables)

collect (*questions*, *all_=True*, *co_constraints=True*)

collects the questions in self.

questions is an OrderedSet of Expression Questions are the terms and the simplest sub-formula that can be evaluated. *collect* uses the simplified version of the expression.

`all=False` : ignore expanded formulas and AppliedSymbol interpreted in a structure `co_constraints=False`
 : ignore `co_constraints`

default implementation for UnappliedSymbol, IfExpr, AUnary, Variable, Number_constant, Brackets

collect_symbols (*symbols=None, co_constraints=True*)
 returns the list of symbol declarations in self, ignoring type constraints
 returns Dict[name, Declaration]

collect_nested_symbols (*symbols, is_nested*)
 returns the set of symbol declarations that occur (in)directly under an aggregate or some nested term, where `is_nested` is flipped to True the moment we reach such an expression
 returns {SymbolDeclaration}

generate_constructors (*constructors: dict*)
 fills the list *constructors* with all constructors belonging to open types.

add_level_mapping (*level_symbols, head, pos_justification, polarity*)

Returns an expression where level mapping atoms (e.g., `lvl_p > lvl_q`) are added to atoms containing recursive symbols.

Parameters

- **level_symbols** (-) – the level mapping symbols as well as their corresponding recursive symbols
- **head** (-) – head of the rule we are adding level mapping symbols to.
- **pos_justification** (-) – whether we are adding symbols to the direct positive justification (e.g., `head => body`) or direct negative justification (e.g., `body => head`) part of the rule.
- **polarity** (-) – whether the current expression occurs under negation.

Returns Expression

substitute (*e0, e1, assignments, tag=None*)
 recursively substitute `e0` by `e1` in self

class `idp_engine.Expression.UnappliedSymbol` (***kwargs*)
 Bases: `idp_engine.Expression.Expression`

The result of parsing a symbol not applied to arguments. Can be a constructor or a quantified variable.

Variables are converted to `Variable()` by `annotate()`.

classmethod construct (*constructor: idp_engine.Expression.Constructor*)
 Create an UnappliedSymbol from a constructor

class `idp_engine.Expression.Variable` (***kwargs*)
 Bases: `idp_engine.Expression.Expression`

AST node for a variable in a quantification or aggregate

copy ()
 create a deep copy (except for rigid terms and variables)

annotatel ()
 annotations that are common to `__init__` and `make()`

class `idp_engine.Expression.Number` (***kwargs*)
 Bases: `idp_engine.Expression.Expression`

```
real ()
    converts the INT number to REAL
```

```
class idp_engine.Expression.Brackets (**kwargs)
    Bases: idp_engine.Expression.Expression
```

6.2.3 idp_engine.Annotate

Methods to annotate the Abstract Syntax Tree (AST) of an IDP-Z3 program.

```
idp_engine.Annotate.get_instantiables (self, for_explain=False)
    compute Definition.instantiables, with level-mapping if definition is inductive
```

Uses implications instead of equivalence if *for_explain* is True

Example: $\{ p() \leftarrow q(). p() \leftarrow r(). \}$ Result when not for_explain: $p() \Leftrightarrow q() \mid r()$ Result when for_explain : $p() \Leftarrow q(). p() \Leftarrow r(). p() \Rightarrow (q() \mid r()).$

Parameters *for_explain* (*Bool*) – Use implications instead of equivalence, for rule-specific explanations

```
idp_engine.Annotate.rename_args (self, new_vars)
    for Clark's completion input : '!v: f(args) <- body(args)' output: '!nv: f(nv) <- nv=args & body(args)'
```

6.2.4 idp_engine.Interpret

Methods to interpret a theory in a data structure

- substitute a constant by its value in an expression
- replace symbols interpreted in a structure by their interpretation
- expand quantifiers

This module also includes methods to:

- substitute an node by another in an AST tree
- instantiate an expression, i.e. replace a variable by a value

This module monkey-patches the ASTNode class and sub-classes.

(see docs/zettlr/Substitute.md)

```
idp_engine.Interpret.add_def_constraints (self, instantiables, problem, result)
    result is updated with the constraints for this definition.
```

The *instantiables* (of the definition) are expanded in *problem*.

Parameters

- **instantiables** (*dict* [*SymbolDeclaration*, *list* [*Expression*]]) – the constraints without the quantification
- **problem** (*Problem*) – contains the structure for the expansion/interpretation of the constraints
- **result** (*dict* [*SymbolDeclaration*, *Definition*, *list* [*Expression*]]) – a mapping from (Symbol, Definition) to the list of constraints

6.2.5 idp_engine.Simplify

Methods to simplify a logic expression.

This module monkey-patches the Expression class and sub-classes.

`idp_engine.Simplify.join_set_conditions` (*assignments: List[idp_engine.Assignments.Assignment]*)
 → *List[idp_engine.Assignments.Assignment]*

In a list of assignments, merge assignments that are set-conditions on the same term.

An equality and a membership predicate (*in* operator) are both set-conditions.

Parameters `assignments` (*List [Assignment]*) – the list of assignments to make more compact

Returns the compacted list of assignments

Return type *List[Assignment]*

6.2.6 idp_engine.Propagate

Computes the consequences of an expression, i.e., the sub-expressions that are necessarily true (or false) if the expression is true (or false)

It has 2 parts: * symbolic propagation * Z3 propagation

This module monkey-patches the Expression and Problem classes and sub-classes.

`idp_engine.Propagate.simplify_with` (*self: idp_engine.Expression.Expression, assignments: idp_engine.Assignments.Assignments*) →
 idp_engine.Expression.Expression
 simplify the expression using the assignments

6.2.7 idp_engine.idp_to_Z3

Translates AST tree to Z3

TODO: vocabulary

6.2.8 idp_engine.Problem

Class to represent a collection of theory and structure blocks.

class `idp_engine.Problem.Propagation` (*value*)
 Describe propagation method

class `idp_engine.Problem.Problem` (**blocks, extended=False*)
 A collection of theory and structure blocks.

extended

True when the truth value of inequalities and quantified formula is of interest (e.g. in the Interactive Consultant)

Type Bool

declarations

the list of type and symbol declarations

Type dict[str, Type]

constraints

a set of assertions.

Type *OrderedSet*

assignments

the set of assignments. The assignments are updated by the different steps of the problem resolution. Assignments include inequalities and quantified formula when the problem is extended

Type *Assignment*

definitions

a list of definitions in this problem

Type [*Definition*]

def_constraints

A mapping of defined symbol to the whole-domain constraints equivalent to its definition.

Type dict[*SymbolDeclaration*, *Definition*], list[*Expression*]

interpretations

A mapping of enumerated symbols to their interpretation.

Type dict[string, *SymbolInterpretation*]

goals

A set of goal symbols

Type dict[string, *SymbolDeclaration*]

_constraintz

a list of assertions, co_constraints and definitions in Z3 form

Type List(*ExprRef*), Optional

_formula

the Z3 formula that represents the problem (assertions, co_constraints, definitions and assignments).

Type *ExprRef*, optional

co_constraints

the set of co_constraints in the problem.

Type *OrderedSet*

propagated

true if a propagation has been done

Type Bool

assigned

set of questions asserted since last propagate

Type *OrderedSet*

cleared

set of questions unassigned since last propagate

Type *OrderedSet*

propagate_success

whether the last propagate call failed or not

Type Bool

z3

mapping from string of the code to Z3 expression, to avoid recomputing it

Type dict[str, ExprRef]**ctx**

Z3 context

classmethod make (*theories, structures, extended=False*)

polymorphic creation

assert_ (*code: str, value: Any, status: idp_engine.Assignments.Status = <Status.GIVEN: 2>*)

asserts that an expression has a value (or not)

Parameters

- **code** (*str*) – the code of the expression, e.g., “p()”
- **value** (*Any*) – a Python value, e.g., True
- **status** (*Status, Optional*) – how the value was obtained. Default: S.GIVEN

constraintz ()

list of constraints, co_constraints and definitions in Z3 form

formula ()

the formula encoding the knowledge base

expand (*max=10, complete=False*)

output: a list of Assignments, ending with a string

symbolic_propagate (*tag=<Status.UNIVERSAL: 4>*)

determine the immediate consequences of the constraints

propagate (*tag=<Status.CONSEQUENCE: 6>, method=<Propagation.DEFAULT: 1>*)

determine all the consequences of the constraints

get_range (*term: str*)

Returns a list of the possible values of the term.

explain (*consequence=None*)

Pre: the problem is UNSAT (under the negation of the consequence if not None)

Returns the facts and laws that make the problem UNSAT.

Parameters

- **self** (*Problem*) – the problem state
- **consequence** (*string | None*) – the code of the sentence to be explained. Must be a key in self.assignments

Returns list of facts and laws that explain the consequence**Return type** (facts, laws) (List[Assignment], List[Expression])**simplify** ()

returns a simpler copy of the Problem, using known assignments

Assignments obtained by propagation become fixed constraints.

decision_table (*goal_string=", timeout=20, max_rows=50, first_hit=True, verify=False*)returns a decision table for *goal_string*, given *self*.**Parameters**

- **goal_string** (*str, optional*) – the last column of the table.

- **timeout** (*int, optional*) – maximum duration in seconds. Defaults to 20.
- **max_rows** (*int, optional*) – maximum number of rows. Defaults to 50.
- **first_hit** (*bool, optional*) – requested hit-policy. Defaults to True.
- **verify** (*bool, optional*) – request verification of table completeness. Defaults to False

Returns the non-empty cells of the decision table

Return type list(list(*Assignment*))

6.2.9 idp_engine.Assignments

Classes to store assignments of values to questions

class `idp_engine.Assignments.Status` (*value*)

Describes how the value of a question was obtained

class `idp_engine.Assignments.Assignment` (*sentence: idp_engine.Expression.Expression, value: Optional[idp_engine.Expression.Expression], status: Optional[idp_engine.Assignments.Status], relevant: Optional[bool] = True*)

Represent the assignment of a value to a question. Questions can be:

- predicates and functions applied to arguments,
- comparisons,
- outermost quantified expressions

A value is a rigid term.

An assignment also has a reference to the symbol under which it should be displayed.

sentence

the question to be assigned a value

Type *Expression*

value

a rigid term

Type *Expression*, optional

status

qualifies how the value was obtained

Type *Status*, optional

relevant

states whether the sentence is relevant

Type *bool*, optional

symbol_decl

declaration of the symbol under which

Type *SymbolDeclaration*

it should be displayed in the IC.

same_as (*other: idp_engine.Assignments.Assignment*) → *bool*

returns True if self has the same sentence and truth value as other.

Parameters *other* (*Assignment*) – an assignment

Returns True if self has the same sentence and truth value as other.

Return type bool

negate ()

returns an Assignment for the same sentence, but an opposite truth value.

Raises **AssertionError** – Cannot negate a non-boolean assignment

Returns returns an Assignment for the same sentence, but an opposite truth value.

Return type [type]

as_set_condition ()

returns an equivalent set condition, or None

Returns meaning “appSymb is (not) in enumeration”

Return type *Tuple*[Optional[*AppliedSymbol*], Optional[bool], Optional[*Enumeration*]]

unset ()

Unsets the value of an assignment.

Returns None

class *idp_engine.Assignments.Assignments* (*arg, **kw)

Contains a set of Assignment

copy () → a shallow copy of D

6.2.10 *idp_engine.Run*

Classes to execute the main block of an IDP program

idp_engine.Run.model_check (*theories*, *structures=None*)

output: “sat”, “unsat” or “unknown”

idp_engine.Run.model_expand (*theories*, *structures=None*, *max=10*, *complete=False*, *extended=False*, *sort=False*)

output: a list of Assignments, ending with a string

idp_engine.Run.model_propagate (*theories*, *structures=None*, *sort=False*)

output: a list of Assignment

idp_engine.Run.decision_table (*theories*, *structures=None*, *goal_string=""*, *timeout=20*, *max_rows=50*, *first_hit=True*, *verify=False*)

returns a decision table for *goal_string*, given *theories* and *structures*.

Parameters

- **goal_string** (*str*, *optional*) – the last column of the table.
- **timeout** (*int*, *optional*) – maximum duration in seconds. Defaults to 20.
- **max_rows** (*int*, *optional*) – maximum number of rows. Defaults to 50.
- **first_hit** (*bool*, *optional*) – requested hit-policy. Defaults to True.
- **verify** (*bool*, *optional*) – request verification of table completeness. Defaults to False

Yields *str* – a textual representation of each rule

`idp_engine.Run.duration(msg="")`
Returns the processing time since the last call to `duration()`, or since the beginning of execution

`idp_engine.Run.execute(self)`
Execute the IDP program

6.2.11 idp_engine.utils

Various utilities (in particular, `OrderedSet`)

class `idp_engine.utils.Semantics` (*value*)
Semantics for inductive definitions

`idp_engine.utils.DEF_SEMANTICS = <Semantics.WELLFOUNDED: 3>`
String constants

`idp_engine.utils.DEFAULT = 'default'`
Module that monkey-patches json module when it's imported so `JSONEncoder.default()` automatically checks for a special "to_json()" method and uses it to encode the object if found.

exception `idp_engine.utils.IDPZ3Error`
raised whenever an error occurs in the conversion from AST to Z3

class `idp_engine.utils.OrderedSet` (*els=[]*)
a list of expressions without duplicates (first-in is selected)

pop (*k*, *d*) → *v*, remove specified key and return the corresponding value.
If key is not found, *d* is returned if given, otherwise `KeyError` is raised

6.3 idp_server module

6.3.1 idp_server.Inferences

This module contains the logic for inferences that are specific for the Interactive Consultant.

`idp_server.Inferences.split_constraints` (*constraints: idp_engine.utils.OrderedSet*) → *idp_engine.utils.OrderedSet*
replace [..., a b, ..] by [..., a, b, ..]

This is to avoid dependencies between a and b (see issue #95).

Parameters `constraints` (`OrderedSet`) – set of constraints that may contain conjunctions

Returns set of constraints without top-level conjunctions

Return type `OrderedSet`

`idp_server.Inferences.get_relevant_questions` (*self: State*)
sets 'relevant in self.assignments sets rank of symbols in self.relevant_symbols removes irrelevant constraints in self.constraints

6.3.2 idp_server.IO

This module contains code to create and analyze messages to/from the web client.

`idp_server.IO.metaJSON (state)`

Format a response to meta request.

Parameters `idp` – the response

Returns out a meta request

`idp_server.IO.load_json (state: idp_engine.Problem.Problem, jsonstr: str)`

Parse a json string and update assignments in a state accordingly.

Parameters

- **state** – a Problem object containing the concepts that appear in the json
- **jsonstr** – the user's assignments in json

Returns the assignments

Return type `idp_engine.Assignments`

6.3.3 idp_server.rest

This module implements the IDP-Z3 web server

To profile it, set `with_profiling` to True

class `idp_server.rest.HelloWorld`

`idp_server.rest.idpOf (code)`

Function to retrieve an IDP object for IDP code. If the object doesn't exist yet, we create it. *idps* is a dict which contains an IDP object for each IDP code. This way, easy caching can be achieved.

Parameters `code` – the IDP code.

Returns IDP the IDP object.

class `idp_server.rest.run`

Class which handles the run. <<Explanation of what the run is here.>>

Parameters Resource – <<explanation of resource>>

post ()

Method to run an IDP program with a procedure block.

:returns stdout.

class `idp_server.rest.meta`

Class which handles the meta. <<Explanation of what the meta is here.>>

Parameters Resource – <<explanation of resource>>

post ()

Method to export the metaJSON from the resource.

Returns metaJSON a json string containing the meta.

class `idp_server.rest.metaWithGraph`

post ()

Method to export the metaJSON from the resource.

Returns metaJSON a json string containing the meta.

```
class idp_server.rest.eval
```

```
class idp_server.rest.evalWithGraph
```

6.3.4 idp_server.State

Management of the State of problem solving with the Interactive Consultant.

```
class idp_server.State.State (idp: idp_engine.Parse.IDP)
```

Contains a state of problem solving

```
classmethod make (idp: idp_engine.Parse.IDP, previous_active: str, jsonstr: str) →  
                  idp_server.State.State
```

Manage the cache of State

Parameters

- **idp** (*IDP*) – idp source code
- **previous_active** (*str*) – previous input from client
- **jsonstr** (*str*) – input from client

Returns a State

Return type *State*

```
add_given (jsonstr: str)
```

Add the assignments that the user gave through the interface. These are in the form of a json string.

Parameters **jsonstr** – the user's assignment in json

Returns the state with the jsonstr added

Return type *State*

**CHAPTER
SEVEN**

INDEX

INDICES AND TABLES

- *Index*
- search

PYTHON MODULE INDEX

i

- `idp_engine.Annotate`, 44
- `idp_engine.Assignments`, 48
- `idp_engine.Expression`, 34
- `idp_engine.Idp_to_Z3`, 45
- `idp_engine.Interpret`, 44
- `idp_engine.Parse`, 30
- `idp_engine.Problem`, 45
- `idp_engine.Propagate`, 45
- `idp_engine.Run`, 49
- `idp_engine.Simplify`, 45
- `idp_engine.utils`, 50
- `idp_server.Inferences`, 50
- `idp_server.IO`, 51
- `idp_server.rest`, 51
- `idp_server.State`, 52

Symbols

`_constraintz` (*idp_engine.Problem.Problem attribute*), 46
`_formula` (*idp_engine.Problem.Problem attribute*), 46

A

`AAggregate` (*class in idp_engine.Expression*), 42
`AComparison` (*class in idp_engine.Expression*), 41
`AConjunction` (*class in idp_engine.Expression*), 41
`add_def_constraints()`
 (*idp_engine.Parse.Definition method*), 33
`add_def_constraints()` (in module *idp_engine.Interpret*), 44
`add_given()` (*idp_server.State.State method*), 52
`add_level_mapping()`
 (*idp_engine.Expression.AImplication method*), 40
`add_level_mapping()`
 (*idp_engine.Expression.AppliedSymbol method*), 43
`add_level_mapping()`
 (*idp_engine.Expression.ARImplication method*), 41
`add_level_mapping()`
 (*idp_engine.Expression.AUnary method*), 41
`add_level_mapping()`
 (*idp_engine.Expression.Expression method*), 37
`add_voc_to_block()`
 (*idp_engine.Parse.Vocabulary method*), 31
`ADisjunction` (*class in idp_engine.Expression*), 41
`AEquivalence` (*class in idp_engine.Expression*), 40
`AImplication` (*class in idp_engine.Expression*), 40
`AMultDiv` (*class in idp_engine.Expression*), 41
`annotate()` (*idp_engine.Expression.Expression method*), 38
`annotate()` (*idp_engine.Parse.Structure method*), 34
`annotatel()` (*idp_engine.Expression.Expression method*), 38
`annotatel()` (*idp_engine.Expression.Variable method*), 43

`annotation` (*vocabulary*), 22
`Annotations` (*class in idp_engine.Parse*), 31
`annotations` (*idp_engine.Expression.Expression attribute*), 35
`annotations` (*idp_engine.Parse.SymbolDeclaration attribute*), 31
`APower` (*class in idp_engine.Expression*), 41
`AppliedSymbol` (*class in idp_engine.Expression*), 42
`AQuantification` (*class in idp_engine.Expression*), 39
`ARImplication` (*class in idp_engine.Expression*), 41
`arity` (*idp_engine.Expression.Constructor attribute*), 38
`arity` (*idp_engine.Expression.Quantee attribute*), 39
`arity` (*idp_engine.Parse.SymbolDeclaration attribute*), 31
`as_set_condition()`
 (*idp_engine.Assignments.Assignment method*), 49
`as_set_condition()`
 (*idp_engine.Expression.Expression method*), 37
`assert_()` (*idp_engine.Problem.Problem method*), 47
`assigned` (*idp_engine.Problem.Problem attribute*), 46
`Assignment` (*class in idp_engine.Assignments*), 48
`Assignments` (*class in idp_engine.Assignments*), 49
`assignments` (*idp_engine.Problem.Problem attribute*), 46
`ASTNode` (*class in idp_engine.Expression*), 34
`ASumMinus` (*class in idp_engine.Expression*), 41
`AUnary` (*class in idp_engine.Expression*), 41

B

`Brackets` (*class in idp_engine.Expression*), 44

C

`check()` (*idp_engine.Expression.ASTNode method*), 34
`cleared` (*idp_engine.Problem.Problem attribute*), 46
`co_constraint` (*idp_engine.Expression.Expression attribute*), 35
`co_constraints` (*idp_engine.Problem.Problem attribute*), 46

`co_constraints()` (*idp_engine.Expression.Expression* `copy()` (*idp_engine.Assignments.Assignments* `method`), 36
`code` (*idp_engine.Expression.Expression* `attribute`), 35
`collect()` (*idp_engine.Expression.AAggregate* `method`), 42
`collect()` (*idp_engine.Expression.AppliedSymbol* `method`), 42
`collect()` (*idp_engine.Expression.AQuantification* `method`), 39
`collect()` (*idp_engine.Expression.Expression* `method`), 36
`collect()` (*idp_engine.Expression.Operator* `method`), 40
`collect_nested_symbols()` (*idp_engine.Expression.AAggregate* `method`), 42
`collect_nested_symbols()` (*idp_engine.Expression.AppliedSymbol* `method`), 43
`collect_nested_symbols()` (*idp_engine.Expression.Expression* `method`), 36
`collect_nested_symbols()` (*idp_engine.Expression.IfExpr* `method`), 39
`collect_nested_symbols()` (*idp_engine.Expression.Operator* `method`), 40
`collect_symbols()` (*idp_engine.Expression.AAggregate* `method`), 42
`collect_symbols()` (*idp_engine.Expression.AppliedSymbol* `method`), 43
`collect_symbols()` (*idp_engine.Expression.AQuantification* `method`), 40
`collect_symbols()` (*idp_engine.Expression.Expression* `method`), 36
`constant`, 7
`constraint`, 8
`constraints` (*idp_engine.Problem.Problem* `attribute`), 45
`constraintz()` (*idp_engine.Problem.Problem* `method`), 47
`construct()` (*idp_engine.Expression.UnappliedSymbol* `class method`), 43
`constructor`, 6
`Constructor` (*class in idp_engine.Expression*), 38
`constructors` (*idp_engine.Parse.Enumeration* `attribute`), 34
`contains()` (*idp_engine.Parse.Enumeration* `method`), 34
`copy()` (*idp_engine.Assignments.Assignments* `method`), 49
`copy()` (*idp_engine.Expression.AAggregate* `method`), 42
`copy()` (*idp_engine.Expression.AppliedSymbol* `method`), 42
`copy()` (*idp_engine.Expression.AQuantification* `method`), 39
`copy()` (*idp_engine.Expression.Expression* `method`), 36
`copy()` (*idp_engine.Expression.Variable* `method`), 43
`ctx` (*idp_engine.Problem.Problem* `attribute`), 47

D

`decision_table()` (*idp_engine.Problem.Problem* `method`), 47
`decision_table()` (*in module idp_engine.Run*), 49
`declarations` (*idp_engine.Problem.Problem* `attribute`), 45
`dedup_nodes()` (*idp_engine.Expression.ASTNode* `method`), 35
`def_constraints` (*idp_engine.Problem.Problem* `attribute`), 46
`DEF_SEMANTICS` (*in module idp_engine.utils*), 50
`DEFAULT` (*in module idp_engine.utils*), 50
`default structure`, 23
`definition`, 10
`Definition` (*class in idp_engine.Parse*), 32
`definitions` (*idp_engine.Problem.Problem* `attribute`), 46
`Display` (*class in idp_engine.Parse*), 34
`display block`, 21
`domain` (*idp_engine.Parse.SymbolDeclaration* `attribute`), 32
`duration()` (*in module idp_engine.Run*), 49

E

`Enumeration` (*class in idp_engine.Parse*), 34
`environment`, 22
`eval` (*class in idp_server.rest*), 52
`evalWithGraph` (*class in idp_server.rest*), 52
`execute()` (*idp_engine.Parse.IDP* `method`), 30
`execute()` (*in module idp_engine.Run*), 50
`expand()` (*idp_engine.Problem.Problem* `method`), 47
`expanded view`, 21
`explain()` (*idp_engine.Problem.Problem* `method`), 47
`Expression` (*class in idp_engine.Expression*), 35
`extended` (*idp_engine.Problem.Problem* `attribute`), 45
`Extern` (*class in idp_engine.Parse*), 31

F

`formula()` (*idp_engine.Problem.Problem* `method`), 47
`fresh_vars` (*idp_engine.Expression.Expression* `attribute`), 36

- from_file() (*idp_engine.Parse.IDP class method*), 30
 from_str() (*idp_engine.Parse.IDP class method*), 30
 function, 6
- ## G
- generate_constructors() (*idp_engine.Expression.AppliedSymbol method*), 43
 generate_constructors() (*idp_engine.Expression.Expression method*), 36
 get_blocks() (*idp_engine.Parse.IDP method*), 30
 get_instantiables() (*idp_engine.Parse.Definition method*), 33
 get_instantiables() (in module *idp_engine.Annotate*), 44
 get_range() (*idp_engine.Problem.Problem method*), 47
 get_relevant_questions() (in module *idp_server.Inferences*), 50
 goals (*idp_engine.Problem.Problem attribute*), 46
- ## H
- heading (*idp_engine.Parse.SymbolDeclaration attribute*), 32
 HelloWorld (*class in idp_server.rest*), 51
- ## I
- IDP (*class in idp_engine.Parse*), 30
 IDP3, 12
 idp_engine.Annotate module, 44
 idp_engine.Assignments module, 48
 idp_engine.Expression module, 34
 idp_engine.Idp_to_Z3 module, 45
 idp_engine.Interpret module, 44
 idp_engine.Parse module, 30
 idp_engine.Problem module, 45
 idp_engine.Propagate module, 45
 idp_engine.Run module, 49
 idp_engine.Simplify module, 45
 idp_engine.utils module, 50
 idp_server.Inferences module, 50
 idp_server.IO module, 51
 idp_server.rest module, 51
 idp_server.State module, 52
 idpOf() (in module *idp_server.rest*), 51
 IDPZ3Error, 50
 IfExpr (*class in idp_engine.Expression*), 39
 include vocabulary, 7
 Installation, 1
 instances (*idp_engine.Parse.SymbolDeclaration attribute*), 32
 instantiate() (*idp_engine.Expression.Expression method*), 37
 instantiate1() (*idp_engine.Expression.Expression method*), 37
 instantiate_definition() (*idp_engine.Parse.Rule method*), 33
 intended meaning, 22
 Interactive Consultant, 1
 interpret() (*idp_engine.Expression.AQuantification method*), 40
 interpret() (*idp_engine.Expression.Expression method*), 38
 interpret() (*idp_engine.Parse.Definition method*), 33
 interpretations (*idp_engine.Problem.Problem attribute*), 46
 is_assignment() (*idp_engine.Expression.AComparison method*), 41
 is_assignment() (*idp_engine.Expression.Expression method*), 36
 is_type_constraint_for (*idp_engine.Expression.Expression attribute*), 36
- ## J
- join_set_conditions() (in module *idp_engine.Simplify*), 45
- ## L
- load_json() (in module *idp_server.IO*), 51
- ## M
- main block, 11
 make() (*idp_engine.Expression.AQuantification class method*), 39
 make() (*idp_engine.Expression.Operator class method*), 40
 make() (*idp_engine.Problem.Problem class method*), 47
 make() (*idp_server.State.State class method*), 52
 meta (*class in idp_server.rest*), 51

metaJSON() (in module *idp_server.IO*), 51
 metaWithGraph (class in *idp_server.rest*), 51
 model_check() (in module *idp_engine.Run*), 49
 model_expand() (in module *idp_engine.Run*), 49
 model_propagate() (in module *idp_engine.Run*), 49
 module
 idp_engine.Annotate, 44
 idp_engine.Assignments, 48
 idp_engine.Expression, 34
 idp_engine.Idp_to_Z3, 45
 idp_engine.Interpret, 44
 idp_engine.Parse, 30
 idp_engine.Problem, 45
 idp_engine.Propagate, 45
 idp_engine.Run, 49
 idp_engine.Simplify, 45
 idp_engine.utils, 50
 idp_server.Inferences, 50
 idp_server.IO, 51
 idp_server.rest, 51
 idp_server.State, 52

N

name (*idp_engine.Expression.Constructor* attribute), 38
 name (*idp_engine.Parse.Symbol* attribute), 32
 name (*idp_engine.Parse.SymbolDeclaration* attribute), 31
 negate() (*idp_engine.Assignments.Assignment* method), 49
 Number (class in *idp_engine.Expression*), 43

O

Operator (class in *idp_engine.Expression*), 40
 OrderedSet (class in *idp_engine.utils*), 50
 original (*idp_engine.Expression.Expression* attribute), 36
 out (*idp_engine.Parse.SymbolDeclaration* attribute), 32

P

parse() (*idp_engine.Parse.IDP* class method), 30
 pop() (*idp_engine.utils.OrderedSet* method), 50
 post() (*idp_server.rest.meta* method), 51
 post() (*idp_server.rest.metaWithGraph* method), 51
 post() (*idp_server.rest.run* method), 51
 predicate, 7
 private (*idp_engine.Parse.SymbolDeclaration* attribute), 32
 Problem (class in *idp_engine.Problem*), 45
 Procedure (class in *idp_engine.Parse*), 34
 propagate() (*idp_engine.Problem.Problem* method), 47
 propagate1() (*idp_engine.Expression.Expression* method), 37

propagate_success (*idp_engine.Problem.Problem* attribute), 46
 propagated (*idp_engine.Problem.Problem* attribute), 46
 Propagation (class in *idp_engine.Problem*), 45
 proposition, 7
 Python API, 15

Q

Quantee (class in *idp_engine.Expression*), 39
 quantifier expression, 9

R

range (*idp_engine.Parse.SymbolDeclaration* attribute), 32
 real() (*idp_engine.Expression.Number* method), 43
 relevant (*idp_engine.Assignments.Assignment* attribute), 48
 rename_args() (*idp_engine.Parse.Rule* method), 34
 rename_args() (in module *idp_engine.Annotate*), 44
 rule, 10
 Rule (class in *idp_engine.Parse*), 33
 run (class in *idp_server.rest*), 51

S

same_as() (*idp_engine.Assignments.Assignment* method), 48
 Semantics (class in *idp_engine.utils*), 50
 sentence, 8
 sentence (*idp_engine.Assignments.Assignment* attribute), 48
 set_level_symbols() (*idp_engine.Parse.Definition* method), 33
 Shebang, 5
 simpler (*idp_engine.Expression.Expression* attribute), 35
 simplify() (*idp_engine.Problem.Problem* method), 47
 simplify_with() (*idp_engine.Expression.Expression* method), 37
 simplify_with() (in module *idp_engine.Propagate*), 45
 sorts (*idp_engine.Expression.Constructor* attribute), 38
 sorts (*idp_engine.Parse.SymbolDeclaration* attribute), 31
 split_constraints() (in module *idp_server.Inferences*), 50
 split_equivalences() (*idp_engine.Expression.AEquivalence* method), 41
 split_equivalences() (*idp_engine.Expression.Expression* method), 37

- State (class in *idp_server.State*), 52
 Status (class in *idp_engine.Assignments*), 48
 status (*idp_engine.Assignments.Assignment* attribute), 48
 structure, 10
 Structure (class in *idp_engine.Parse*), 34
 sub_exprs (*idp_engine.Expression.Expression* attribute), 35
 sub_exprs (*idp_engine.Expression.Quantee* attribute), 39
 substitute () (*idp_engine.Expression.AppliedSymbol* method), 43
 substitute () (*idp_engine.Expression.Expression* method), 36
 symbol, 6
 Symbol (class in *idp_engine.Parse*), 32
 symbol (*idp_engine.Expression.Constructor* attribute), 39
 symbol_decl (*idp_engine.Assignments.Assignment* attribute), 48
 SymbolDeclaration (class in *idp_engine.Parse*), 31
 symbolic_propagate () (*idp_engine.Expression.Expression* method), 37
 symbolic_propagate () (*idp_engine.Problem.Problem* method), 47
 symbols (*idp_engine.Parse.SymbolDeclaration* attribute), 31
- ## T
- term, 8
 tester (*idp_engine.Expression.Constructor* attribute), 38
 theory, 7
 Theory (class in *idp_engine.Parse*), 32
 translate () (*idp_engine.Expression.Expression* method), 37
 translate1 () (*idp_engine.Expression.IfExpr* method), 39
 Tuple (class in *idp_engine.Parse*), 34
 tuples (*idp_engine.Parse.Enumeration* attribute), 34
 type, 6
 type (*idp_engine.Expression.Constructor* attribute), 38
 type (*idp_engine.Expression.Expression* attribute), 35
 type (*idp_engine.Parse.SymbolDeclaration* attribute), 32
 TypeDeclaration (class in *idp_engine.Parse*), 31
- ## U
- UnappliedSymbol (class in *idp_engine.Expression*), 43
 unit (*idp_engine.Parse.SymbolDeclaration* attribute), 32
- unset () (*idp_engine.Assignments.Assignment* method), 49
 update_exprs () (*idp_engine.Expression.Expression* method), 36
- ## V
- value (*idp_engine.Assignments.Assignment* attribute), 48
 value (*idp_engine.Expression.Expression* attribute), 35
 Variable (class in *idp_engine.Expression*), 43
 vars (*idp_engine.Expression.Quantee* attribute), 39
 vocabulary, 6
 Vocabulary (class in *idp_engine.Parse*), 30
- ## Z
- z3 (*idp_engine.Problem.Problem* attribute), 46